

the general position is $\pm(x, y, z; \bar{x}, \bar{y}, \frac{1}{2}+z; \bar{y}, x, \frac{3}{4}+z; y, \bar{x}, \frac{1}{4}+z)$ and let us find the phase relation corresponding to the symmetry operation $\mathbf{r}(xyz) \rightarrow \mathbf{r}'(\bar{y}, x, \frac{3}{4}+z)$.

This is done in four steps.

- (1) Form the scalar product
 $\mathbf{h} \cdot \mathbf{r}' = h(\bar{y}) + kx + l(\frac{3}{4} + z).$
- (2) Isolate the translational component which gives rise to a phase factor $a = \exp 2\pi i \frac{3}{4}l = \exp(3\pi i l/2).$
- (3) Rewrite the resting scalar product in the form $\mathbf{r} \cdot \mathbf{h}' = xk + y(\bar{h}) + zl$, i.e. bring xyz into their usual sequence.
- (4) The desired symmetry relation between structure factors is
 $F(\mathbf{h}) = aF(\mathbf{h}')$, i.e.
 $F(hkl) = \exp(3\pi i l/2)F(k\bar{h}l).$

If the reader is able to show that to the points $\mathbf{r}(xyz)$ and $\mathbf{r}'(\frac{1}{4}-z, \frac{1}{4}-y, x)$ of group $Fd3m(O_h^7)$ No. 227 corresponds the phase relation $F(hkl) = F(l\bar{k}\bar{h})\exp(\pi i(h+k)/2)$ he will probably have understood how to use the method.

The theoretical proof may be found in French (Bertaut, 1959), in English (Bertaut & Waser, 1957) and in German (Bertaut, 1958).

In Jeffery's (1963) notation, the phase relation under (4) reads

$$\alpha_{hkl} = \alpha_{k\bar{h}l} + (3\pi/2)l$$

whereas Jeffery writes

$$\alpha_{hkl} = \alpha_{k\bar{h}l} + (3\pi/2)l.$$

We must conclude and have checked that in Tables 1 and 2 given by Jeffery, $\alpha_{k\bar{h}l}$ should be replaced by $\alpha_{k\bar{h}l}$ and, vice versa, $\alpha_{k\bar{h}l}$ should be replaced by $\alpha_{k\bar{h}l}$.

Finally let us mention that all phase relations for centrosymmetric groups are given in *Tables de Linéarisation des Facteurs de Structure* (Bertaut & Dulac, 1955, 1956).

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Lattice constants of some double sulphates $M_2Co(SO_4)_2 \cdot 6H_2O$. By P. HARTMAN and C. F. WOENSDREGT,
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(Received 9 January 1964)

The lattice constants of four isomorphous cobalt double sulphates $M_2Co(SO_4)_2 \cdot 6H_2O$, with $M = K, Rb, NH_4$, and Cs , have been determined from powder X-ray photographs with a quadruple Guinier-de Wolff camera (de Wolff, 1948) and $Cu K\alpha$ radiation. Because of the larger deviations on the two outer strips, only the inner ones were used, one recording the powder lines of the cobalt double sulphate, the other recording the lines of a reference substance for which we chose potassium aluminium alum. In a separate measurement on a Debye-Scherrer X-ray photograph taken in a cylindrical camera with 9 cm diameter the unit cell edge of the potassium aluminium alum was found to be 12.157 \AA , in excellent agreement with the value $12.158 \pm 0.001 \text{ \AA}$ found by Klug & Alexander (1940).

Calibration of each film was based on this value of the

alum unit cell edge. The measured line positions appeared to be, within the limits of errors, a linear function of the calculated positions.

Irregular deviations as found by Fisher (1957) were not observed.

With this linear function the line positions of the sulphates were corrected and the constants in the relation

$$\sin^2 \theta = Ah^2 + Bk^2 + Cl^2 + Dhl$$

were calculated. B was found from $\sin^2 \theta$ differences between hk_1l and hk_2l reflexions, A from $hk0$ reflexions, C from $0kl$ reflexions and from $\sin^2 \theta$ differences between hkl and $h\bar{k}\bar{l}$ reflexions and D from all hkl reflexions. Table 1 gives the calculated lattice constants with the standard deviation of the mean. The morphological axial ratios were taken from Groth (1908).

Table 1. Lattice constants of $M_2Co(SO_4)_2 \cdot 6H_2O$

	K	Rb	NH ₄	Cs
a_0	$9.061 \pm 0.003 \text{ \AA}$	$9.180 \pm 0.001 \text{ \AA}$	$9.247 \pm 0.001 \text{ \AA}$	$9.316 \pm 0.001 \text{ \AA}$
b_0	12.207 ± 0.001	12.433 ± 0.001	12.519 ± 0.001	12.824 ± 0.001
c_0	6.151 ± 0.002	6.230 ± 0.003	6.239 ± 0.001	6.365 ± 0.002
β	$104^\circ 48' \pm 2'$	$106^\circ 01' \pm 1'$	$107^\circ 02' \pm 1'$	$107^\circ 07' \pm 1'$
β (morph.)	$104^\circ 55'$	$106^\circ 01'$	$106^\circ 56'$	$107^\circ 08'$
Axial ratio	$0.7423:1:0.5039$	$0.7384:1:0.5011$	$0.7386:1:0.4984$	$0.7265:1:0.4963$
Axial ratio (morph.)	$0.7404:1:0.5037$	$0.7391:1:0.5011$	$0.7392:1:0.4985$	$0.7270:1:0.4968$

Table 2. Observed and calculated $10^5 \cdot \sin^2 \theta$ values of $M_2Co(SO_4)_2 \cdot 6H_2O$

M = K				M = Rb				M = NH ₄				M = Cs					
$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$		$10^5 \cdot \sin^2 \theta$			
<i>hkl</i>	obs.	calc.	<i>hkl</i>	obs.	calc.	<i>hkl</i>	obs.	calc.	<i>hkl</i>	obs.	calc.	<i>hkl</i>	obs.	calc.	<i>hkl</i>	obs.	calc.
020	1601	1592	110	1144	1146	020	1518	1514	110	1110	1109						
001	1694	1677	020	1544	1535	001	1670	1667	001	1602	1603						
011	2074	2075	001	1661	1655	011	2048	2046	011	1963	1964						
111	2266	2267	111	2189	2181	111	2148	2146	120	2192	2192						
200	3096	3092	120	2300	2297	120	2276	2273	021	3048	3046						
021	3271	3270	200	3046	3048	200	3033	3036	121	3154	3149						
111	3420	3430	021	3192	3190	021	3182	3181	201	3305	3307						
201	3598	3606	210	3435	3432	121	3282	3281	210	3363	3355						
211	4009	4004	130	4209	4216	201	3378	3385	111	3358	3358						
130	4348	4356	220	4580	4583	111	3470	3464	211	3667	3667						
121	4624	4625	131	5251	5251	211	3766	3764	130	3997	3995						
031	5261	5260	201	5935	5941	130	4170	4166	220	4435	4437						
131	5450	5451	040	6145	6140	220	4558	4550	121	4440	4440						
201	5937	5933	211	6325	6325	121	4600	4599	131	4954	4953						
211	6350	{ 6331	230	6508	6502	221	4895	4899	040	5771	5772						
040	6370	140	6904	6902	031	5078	5074	201	5891	5888							
002	6711	{ 6711	311	7030	7038	131	5174	5174	112	6233	6232						
112	6711	{ 6717	202	7184	7188	201	6020	6021	311	6764	6764						
310	7367	7355	310	7243	7241	040	6061	6056	012	6771	6774						
221	7511	7525	221	7466	7476	211	6399	6400	202	6821	6826						
212	7894	{ 7872	212	7572	7572	112	6491	{ 6488	310	7097	7097						
122	7911	122	7681	7677	131	6492	6492	122	7322	7314							
141	8236	8238	041	7801	7795	140	6815	6815	221	7331	7331						
321	8487	8481	141	7929	7938	311	6899	6900	141	7485	7479						
231	9521	9516	321	8183	8189	202	7068	7069	321	7837	7847						
331	10468	10472	320	8397	8393	310	7211	7210	320	8181	8180						
241	12299	12303	222	8712	8723	221	7535	7537	240	8766	8766						
250	13060	{ 13044	240	9188	9188	122	7621	7624	141	8770	8770						
042	13060	{ 13079	231	9388	9395	321	8033	8034	241	9079	9079						
242	13840	13844	132	9601	{ 9595	112	9120	9124	132	9103	9118						
420	13963	{ 13960	241	9604	{ 9604	231	9429	9428	312	9638	9638						
331	13963	{ 13963	331	10113	10108	312	9929	{ 9925	331	9462	9650						
			051	11258	11249	331	9928	{ 9928	032	9661	9661						
			411	11743	11752	122	10253	10260	122	9896	9896						
			321	11898	11905	241	12082	12078	330	9982	9983						
			132	12068	{ 12073	212	12726	{ 12719	051	10616	{ 10622						
			241	12082	{ 12082	042	12725	{ 12725	311	10637	{ 10637						
			042	12774	{ 12759	340	12884	12887	322	10720	{ 10720						
			341	12794	{ 12794	420	13653	13658	151	10711	{ 10725						
			251	13061	13058				411	11362	11358						
			242	13323	13329												
			420	13722	13726												
			203	14228	{ 14222												
			412	14228	{ 14238												
			003	14881	14891												

Table 2 lists the observed $\sin^2 \theta$ values of the measured reflexions, together with the calculated values.

The crystals were prepared by Mrs. H. Zandbergen of the Kamerlingh Onnes Laboratorium and the X-ray photographs were taken by Mr. A. Verhoorn.

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